An Experimental and Quantum Chemical Investigation of CO Binding to Heme Proteins and Model Systems: A Unified Model Based on ¹³C, ¹⁷O, and ⁵⁷Fe Nuclear Magnetic Resonance and ⁵⁷Fe Mössbauer and Infrared Spectroscopies

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Abstract: We have investigated the question of how CO ligands bind to iron in metalloporphyrins and metalloproteins by using a combination of nuclear magnetic resonance (NMR), ⁵⁷Fe Mössbauer, and infrared spectroscopic techniques, combined with density functional theoretical calculations to analyze the spectroscopic results. The results of ¹³C NMR isotropic chemical shift, ¹³C NMR chemical shift anisotropy, ¹⁷O NMR isotropic chemical shift, ¹⁷O nuclear quadrupole coupling constant, ⁵⁷Fe NMR isotropic chemical shift, ⁵⁷Fe Mössbauer quadrupolar splitting, and infrared measurements indicate that CO binds to Fe in a close to linear fashion in all conformational substates. The 13 C-isotropic shift and shift anisotropy for an A_o substate model compound: Fe(5,10,15,20-tetraphenylporphyrin)(CO)(N-methylimidazole), as well as the ¹⁷O chemical shift, and the 17 O nuclear quadrupole coupling constant (NQCC) are virtually the same as those found in the A_0 substate of *Physeter catodon* CO myoglobin and lead to most probable ligand tilt (τ) and bend (β) angles of 0° and 1° when using a Bayesian probability or Z surface method for structure determination. The infrared $\nu_{\rm CO}$ for the model compound of 1969 cm⁻¹ is also that found for A₀ proteins. Results for the A₁ substate (including the ⁵⁷Fe NMR chemical shift and Mössbauer quadrupole splitting) are also consistent with close to linear and untilted Fe-C-O geometries ($\tau = 4^\circ, \beta = 7^\circ$), with the small changes in ligand spectroscopic parameters being attributed to electrostatic field effects. When taken together, the ¹³C shift, ¹³C shift anisotropy, ¹⁷O shift, ¹⁷O NQCC, ⁵⁷Fe shift, ⁵⁷Fe Mössbauer quadrupole splitting, and ν_{CO} all strongly indicate very close to linear and untilted Fe-C-O geometries for all carbon monoxyheme proteins. These results represent the first detailed quantum chemical analysis of metal-ligand geometries in metalloproteins using up to seven different spectroscopic observables from three types of spectroscopy and suggest a generalized approach to structure determination.

Introduction

How small ligands such as CO, O₂, RNC, RNO, NO, and N_3^- bind to metalloproteins and metalloporphyrins has been a topic of interest for some time,¹⁻⁴ because of the obvious importance of especially O₂ carriers in respiration, and more recently of NO and CO ligands as regulators of cell and organ

function.⁵ Typically, X-ray crystallographic methods have been used to deduce metal-ligand geometries, but quite large variabilities appear to exist between different structures. For example, Fe-C-O bond angles from 176° to 118° have been reported,^{6,7} Fe-O-O angles from 159° to 115° have been described,^{8,9} Fe-C-N angles of 180° to 96° have been observed in alkyl isocyanide adducts,^{10,11} etc., and it is unclear to what extent these differences are real. In the case of CO, the results of infrared and Raman spectroscopy have been used to deduce a close-to-linear and untilted Fe-C-O geometry,^{12,13} with the changes in the observables being attributed to electrostatic field

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effects, much as with our own NMR/IR correlations.14-16 However, very recent crystallographic results on carbonmonoxymyoglobin again suggest distorted (~45-55°) Fe-C-O bonding,17 consistent with earlier crystallographic results7,18 and with XANES and EXAFS results.^{19,20} Distortions have also been suggested from solid-state NMR²¹ and from some Mössbauer work.^{22,23} Given the fact that IR/Raman experiments are more difficult with non-CO ligands, and that the actual detailed assignments themselves are not always simple to make,²⁴ it therefore seems to be desirable to explore the possibilities of using a variety of spectroscopic observables to investigate metal-ligand bonding. In this paper, we use up to six additional spectroscopic parameters, the isotropic carbon-13 NMR chemical shift (δ_i^{13} C), the ¹³C NMR chemical shift anisotropy (CSA) $(\Delta \delta^{13}C)$, the isotropic oxygen-17 NMR chemical shift $(\delta_i^{17}O)$, the ¹⁷O nuclear quadrupole coupling constant (NQCC) ($e^2qO/$ *h*, ¹⁷O), the isotropic iron-57 NMR chemical shift (δ_i ⁵⁷Fe), the iron-57 Mössbauer quadrupole splitting (ΔE_Q , ⁵⁷Fe), and the CO infrared stretch frequency (ν_{CO}), to test various structural models, using parameter surfaces and the Bayesian probability method reported previously for amino acids.^{25,26} The methods described are general and show how NMR, Mössbauer, and IR techniques can all be used together to develop and test models of metal-ligand interactions in metalloproteins, by using quantum chemical methods to make the necessary correlations between the spectroscopic observables and structure.

Experimental Section

Chemical Aspects. The synthesis and characterization of the model compound Fe(5,10,15,20-tetraphenylporphyrin)(CO)(*N*-methylimida-

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zole) will be described in detail elsewhere²⁷ and basically followed standard methods.²⁸ The exception is that two samples were prepared. The first was prepared in a "standard" fashion in that solvent was removed from crystals in vacuo, while in a second sample the mother liquor was retained, in an effort to retain good quality crystals for solidstate NMR. CO (13CO, 99%; Cambridge Isotope Laboratories, Andover, MA; C17O, 37%, Icon Services, Inc., Summit, NJ) gas exchange was achieved prior to crystallization using a Pd/Al₂O₃ heterogeneous catalyst.²⁹ Here, approximately 100 mg Fe(TPP)(CO)(NMeIm) (TPP = 5.10,15,20-tetraphenylporphyrin; NMeIm = N-methylimidazole) was exchanged with ¹³CO or C¹⁷O (~5 mL at STP) in a heptane solvent at 23 °C using 3 mg of Pd (10%) on Al₂O₃ (Alfa Products, Danvers, MA). This catalyst causes essentially statistical (random) exchange in \sim 5 min and can be readily removed by filtration. Crystals were then grown from CH₂Cl₂/pentane using a gradient technique. Crystallization times varied but were typically ~ 5 days.

For protein NMR spectroscopy, we used both horse heart and sperm whale myoglobins (Sigma Chemical Company, St. Louis, MO). For ¹³C and ¹⁷O NMR, we typically purified myoglobin (Mb) by using a Sephadex G25 column and then grew needle or star-shaped crystal clusters from (NH₄)₂SO₄ (83%, pH = 7.0). The crystals were then reduced on a Schlenk line using a few drops of (NH₄)₂ SO₄ solution containing Na₂S₂O₄ (Sigma), and carbonylated with CO gas. Fourier transform infrared spectra were recorded on a Nicolet (Madison, WI) Magna-IR 750 spectrometer in order to deduce substate composition.

The A_o substate of MbCO was produced in ~95% yield by converting Mb into the tetrazole derivative of His $64^{30,31}$ with CNBr (Aldrich Chemical Co., Milwaukee, WI) and NaN₃ (Fisher Scientific, Fair Lawn, NJ). Crystals were grown from (NH₄)₂SO₄, (78%, pH = 6.7) followed by reduction and carbonylation as described above.

Sperm whale MbCO was used for $^{57}{\rm Fe}$ NMR and Mössbauer spectroscopy, and was from the same batch whose preparation has been described previously. 32

Spectroscopic Aspects. Solid-state ¹³C and ¹⁷O NMR spectra were recorded using "home-built" spectrometers, which consist of 8.45 T 3.5 in. bore and 11.7 T 2.0 in. bore superconducting solenoid magnets (Oxford Instruments, Osney Mead, Oxford, U.K.), and Tecmag (Houston, TX) Aries and Libra data systems, together with a variety of other digital and rf circuitries. For rf pulse amplification, we used Amplifier Research (Souderton, PA) and Henry Radio (Los Angeles, CA) transmitters. Solid-state spectra were obtained by using 5 mm Doty Scientific (Columbia, SC) "magic-angle" sample-spinning (MAS) NMR probes, in some cases using sealed Wilmad (Buena, NJ) glass inserts. The 90° pulse widths varied but were typically $\sim 4 \,\mu s$ for ¹³C and 5 μ s (solid 90° pulse) for ¹⁷O. For ¹³C NMR, we typically used ¹H-¹³C cross polarization³³ with nonquaternary suppression.³⁴ Recycle times for ¹³C NMR were typically \sim 2 s, while for ¹⁷O NMR, recycle times varied from 50 ms (A1 MbCO) to 1 s (Fe(TPP)(CO)(NMeIm)). Carbon-13 chemical shifts were referenced with respect to the lowfield peak of adamantane, taken to be 38.5 ppm downfield from external tetramethylsilane, while ¹⁷O spectra were referenced with respect to an external sample of tap water. The convention that high-frequency, low-field, paramagnetic or deshielded shifts are more positive (International Union of Pure and Applied Chemistry, IUPAC, δ scale) was used. Shift tensor elements use the convention that $\delta_{11} \ge \delta_{22} > \delta_{33}$.

The principal components of the chemical shift tensor, δ_{11} , δ_{22} , and δ_{33} , were deduced from the intensities of the individual spinning

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Figure 1. Fragments used for calculations. (A) Fe-C-O model used in electrostatic field calculations. Hyphens represent 0.4*e* point charges located at 2 Å from the Fe atom (the 5 closest nitrogen positions in a heme plus axial base). (B) Fe bis(amidinato)(CO)(*N*-methylimidazole) model system used for ¹³C,¹⁷O shielding calculations. (C) Full porphine model used for iron shift and efg calculations, Fe(porphine)(CO)(*N*methylimidazole).

sidebands using several versions of the Herzfeld-Berger method,³⁵ as described below.

Computational Aspects. We carried out five series of density functional theory (DFT) calculations. In the first, we investigated how uniform and nonuniform electric fields influence the vibrational frequency and the ¹⁷O nuclear quadrupole coupling constant, as an extension of previous and more recent work on ¹³C NMR/¹⁷O NMR/ IR shift correlations.^{14–16,36} These calculations used the small cluster shown in Figure 1A, which facilitated a full E-field vibrational/shift/ electric field gradient (efg) analysis in a reasonable time period. The second set of calculations involved a study of how ligand tilt (τ) and bend (β) alone affect the ¹³C and ¹⁷O shifts and shift anisotropies. This time a much larger model was used (Figure 1B), an Fe bis(amidinato)-(CO)(N-methylimidazole) system, which has been investigated previously by several groups.37,38 Third, we investigated the 57Fe shifts and ⁵⁷Fe Mössbauer quadrupolar splittings (equivalent to a determination of the electric field gradient tensor at the iron nucleus) using a full porphyrin, the Fe(porphinato)(CO)(N-methylimidazole) system shown in Figure 1C. Here, a large system was thought to be essential in order to adequately describe the 57Fe-ligand interactions. We also carried out a series of calculations on several chromium carbonyls and model hemes in which the orientation of the axial base was varied. Finally, we examined the shielding and the localized molecular orbital contributions to shielding at a single (linear) geometry.

The smallest model system is the one recently used to investigate charge field perturbation of ¹³C,¹⁷O shift– ν_{CO} (IR) correlations in proteins,³⁶ and consists of the octahedral arrangement of atoms and point charges shown in Figure 1A. The 0.4e point charges ensure a diamagnetic ground state and electroneutrality and are placed at 2 Å from the Fe atom. We used the deMon program³⁹ to evaluate the ¹⁷O efg and ν_{CO} , employing Wachters' all electron basis set for iron (14s9p5d/8s5p5d)^{40,41} together with an IGLO-III basis for C and O⁴² and the Perdew–Wang (PW91) gradient-corrected exchange-correlation functional.⁴³ The ¹⁷O NQCC and ν_{CO} values were evaluated in the presence of uniform electric fields applied along the Fe–C–O axis, having magnitudes from 0.02 to -0.02 au (1 au field = 5.14225 × 10⁹ V/cm), or in the presence of point changes of ±e at 2 Å from the oxygen, along the Fe–C–O axis.

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We next evaluated the 13C and 17O shieldings and shielding tensor elements, this time as a function of τ and β . Here, the larger Fe bis-(amidinato)(CO)(NMeIm) model shown in Figure 1B was used, since we were more interested in investigating the actual shifts, rather than the correlations between shifts and $\nu_{\rm CO}$, and the elimination of the full vibrational analysis made computation of a shielding surface containing 35 τ , β values feasible. The nuclear shieldings were calculated with the sum-over-states density functional perturbation theory (SOS-DFPT) approach in its LOC1 approximation⁴⁴ using individual gauges for localized orbitals (IGLO)⁴² as implemented in the deMon program.³⁹ We used the same iron basis as that shown above, while the C,O basis was reduced to IGLO-II.42 Next, we investigated 57Fe NMR chemical shifts and the electric field gradients at ¹⁷O, and ⁵⁷Fe (directly related to the ⁵⁷Fe Mössbauer quadrupole splittings, ΔE_0), again as a function of ligand tilt and bend. Since metal shifts have in the past been rather difficult to evaluate, we used a much larger fragment and increased the grid coarseness for our τ,β study. We used a published porphyrin geometry²⁸ minus the C^{β}-substituents, together with an axial imidazole oriented in the same way as reported in the crystal structure of carbonmonoxymyoglobin.45 We carried out geometry optimizations of the Fe-C and C-O bond lengths at fixed ligand tilt and bend angles with the Gaussian 94/DFT program⁴⁶ using the B3LYP hybrid exchange-correlation functional,47 Wachters' (62111111/3311111/3111) Fe basis set,^{40,41} a 6-31G* basis on the carbonyl group and the 5 nitrogen atoms, and a 3-21G basis on the remaining atoms. The nuclear shielding calculations were carried out in Gaussian 94/DFT using gaugeincluding atomic orbitals (GIAO),⁴⁶ a locally dense basis set scheme, and the B3LYP functional.47 Wachters' basis set was used on the iron, 6-311++G(2d) on the CO group and five nitrogen atoms with 6-31G* and 4-31G*, on the second and third atom shells, respectively.

Heme model ligand shielding calculations were also done with G94/ DFT using the BPW91 functional. For Fe(P)(CO)(pyr) (pyr = pyridine), the iron was represented with the LANLD2DZ effective core potential (ECP) with a (42111/2111/311) basis set,⁴⁸ or with the same ECP,⁴⁹ 6-311++G(2d) on the CO group, 6-31G* on the nitrogen atoms, and 3-21G and STO-3G basis sets on the outermost atoms of the porphyrin ring. For Fe(TPP)(CO)(NMeIm), we used Wachters' iron basis set,^{40,41} 6-311++G(2d) on the CO group and the five nitrogen atoms, 6-31G* on the carbons bonded to the nitrogen atoms and 3-21G* on the remaining atoms. For the Fe(C₂Cap)(CO)(NMeIm), we used Wachters' Fe basis set, 6-311++G(2d) on the CO group and 6-31G* on the rest of the atoms. This approach is basically that used by Bühl for ⁵⁷Fe NMR chemical shift calculations in organometallic systems,

(41) Basis sets were obtained from the Extensible Computational Chemistry Environment Basis Set Database, Version 1.0, as developed and distributed by the Molecular Science Computing Facility, Environmental and Molecular Sciences Laboratory, which is part of the Pacific Northwest Laboratory, P.O. Box 999, Richland, WA 99352, and is funded by the U.S. Department of Energy under contract DE-AC06-76RLO 1830. Contact David Feller, Karen Schuchardt, or Don Jones for further information.

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 Table 1.
 ¹³C, ¹⁷O NMR Parameters for Fe Bis(amidinato)(CO)(NMeIm) as a Function of Ligand Tilt and Bend

 ligand geometry
 shielding tensor element

| ligand | geometry | shie | shielding tensor element | | | | |
|------------|------------|--------------------------------|--------------------------|-----------------------|-------------------------------|-------------------------------------|-------------------------------------|
| tilt (deg) | bend (deg) | $\overline{\sigma_{11}}$ (ppm) | σ_{22} (ppm) | σ ₃₃ (ppm) | $\sigma_{\rm i} ({\rm ppm})$ | $ \sigma_{22} - \sigma_{11} $ (ppm) | $ \sigma_{33} - \sigma_{11} $ (ppm) |
| | | | | ¹³ C | | | |
| 0 | 0 | -182.9 | -169.9 | 263.1 | -29.9 | 13 | 446 |
| 20 | 0 | -182.8 -180.1 | -160.8 | 263.2 | -28.8 -25.8 | 10 | 440 444 |
| 30 | 0 | -172.9 | -132.9 | 253.1 | -17.6 | 40 | 426 |
| 40 | 0 | -166.1 | -63.1 | 214.9 | -4.8 | 103 | 381 |
| 50 | 0 | -156.9 | 47.1 | 115.1 | 1.8 | 204 | 272 |
| 0 | 10 | -183.8 | -169.8 | 264.2 | -29.8 | 14 | 448 |
| 20 | 10 | -179.9 -170.9 | -160.9 | 257.1 | -28.2 -24.9 | 10 | 440 |
| 30 | 10 | -160.1 | -141.1 | 246.9 | -18.1 | 19 | 407 |
| 40 | 10 | -151.9 | -77.9 | 212.1 | -5.9 | 74 | 364 |
| 0 | 20 | -183.9 | -168.9 | 270.1 | -27.6 | 15 | 454 |
| 10 | 20 20 | -180.0 -170.8 | -162.0 -155.8 | 260.0 | -27.3 -25.1 | 18 | 440 |
| 30 | 20 | -151.0 | -148.0 | 239.0 | -20.0 | 3 | 390 |
| 40 | 20 | -139.0 | -93.0 | 206.0 | -8.7 | 46 | 345 |
| 0 | 30 | -184.4 | -167.4 | 282.2 | -23.3 | 17 | 467 |
| 10 | 30 | -178.9 | -154.9 | 259.1 | -24.9 | 24 | 438 |
| 20 | 30 30 | -1/5.3 -161.6 | -146.3 -136.6 | 244.7 226.4 | -25.6 -23.9 | 29 25 | 420 |
| 40 | 30 | -128.2 | -109.2 | 191.8 | -15.2 | 19 | 320 |
| 0 | 40 | -184.6 | -161.6 | 290.4 | -18.6 | 23 | 475 |
| 10 | 40 | -174.9 | -137.9 | 244.1 | -22.9 | 37 | 419 |
| 20 | 40 | -179.0 | -136.0 | 231.0 | -28.0 | 43 | 410 |
| 30 40 | 40 | -171.8 -125.7 | -127.8 -121.7 | 199.2 | -33.3 -32.4 | 44 4 | 276 |
| 0 | 50 | -184.9 | -154.9 | 296.1 | -14.6 | 30 | 481 |
| 10 | 50 | -174.9 | -137.9 | 244.1 | -22.9 | 37 | 419 |
| 20 | 50 | -177.8 | -128.8 | 201.2 | -35.1 | 49 | 379 |
| 30 | 50 50 | -171.1 | -120.1 | 135.9 | -51.8 | 51 | 307 |
| 40 | 30 60 | -177.0 | -145.0 | 284.0 | -81.4 -12.7 | 13 32 | 461 |
| 10 | 60 | -170.1 | -131.1 | 217.9 | -27.8 | 39 | 388 |
| 20 | 60 | -160.0 | -120.0 | 139.0 | -47.0 | 40 | 299 |
| 30 | 60 | -148.9 | -121.9 | 7.1 | -87.9 | 27 | 156 |
| | | | | ¹⁷ O | | | |
| 0 | 0 | -346.3 | -323.3 | 410.7 | -86.3 | 23 | 757 |
| 10 | 0 | -345.1 -338.0 | -318.1 -282.0 | 412.9 | -83.4 -72.7 | 27 | 758 740 |
| 30 | 0 | -335.1 | -173.1 | 341.9 | -55.4 | 162 | 677 |
| 40 | 0 | -348.1 | 13.9 | 180.9 | -51.1 | 362 | 529 |
| 50 | 0 | -383.9 | -114.9 | 206.1 | -97.6 | 269 | 590 |
| 0 | 10 | -357.9 -342.6 | -328.9 -313.6 | 417.1 | -89.9 -81.9 | 29 | 775 |
| 20 | 10 | -327.9 | -269.9 | 394.1 | -67.9 | 58 | 733 |
| 30 | 10 | -325.0 | -167.0 | 329.0 | -54.3 | 158 | 654 |
| 40 | 10 | -336.8 | 4.2 | 155.2 | -59.1 | 341 | 492 |
| 0 | 20 | -381.7 | -329.7 | 434.3 | -92.4 | 52 | 816 |
| 20 | 20 | -319.8 | -314.9 -280.8 | 417.1 | -69.1 | 40 | 712 |
| 30 | 20 | -318.1 | -179.1 | 318.9 | -59.4 | 139 | 637 |
| 40 | 20 | -330.2 | -21.2 | 131.8 | -73.2 | 309 | 462 |
| 0 | 30 | -429.6 | -324.2 | 465.6 | -95.9 | 105 | 895 |
| 10 | 30 | -380.3 | -311.3 -202.2 | 429.7 | -87.3 | 69 15 | 810 |
| 20 30 | 30 | -310.9 | -303.2 -212.9 | 312.1 | -70.6 | 98 | 623 |
| 40 | 30 | -322.9 | -60.9 | 112.1 | -90.6 | 262 | 435 |
| 0 | 40 | -489.0 | -319.0 | 503.0 | -101.7 | 170 | 992 |
| 10 | 40 | -425.2 | -305.2 | 444.8 | -95.2 | 120 | 870 |
| 20 | 40 40 | -354.9 | -302.9 -267.9 | 398.1 | -86.6 -87.6 | 52 39 | /55 |
| 40 | 40 | -314.1 | -111.1 | 143.9 | -93.8 | 203 | 458 |
| 0 | 50 | -565.7 | -309.7 | 545.3 | -110.0 | 256 | 1111 |
| 10 | 50 | -487.7 | -299.7 | 457.3 | -110.0 | 188 | 945 |
| 20 | 50 | -423.7 | -300.7 | 400.3 | -108.0 | 123 | 824 |
| 30 40 | 50 50 | -340./ -300.7 | -301./ -174.7 | 333.3 319 3 | -105.0 | 45 126 | 080 620 |
| 0 | 60 | -650.7 | -297.7 | 570.3 | -126.0 | 353 | 1221 |
| 10 | 60 | -564.3 | -295.3 | 457.7 | -134.0 | 269 | 1022 |
| 20 | 60 | -512.0 | -301.0 | 381.0 | -144.0 | 211 | 893 |
| 30 | 60 | -454.0 | -296.0 | 366.0 | -128.0 | 158 | 820 |

Table 2. ⁵⁷Fe NMR Shielding Parameters for FeP(CO)(NMeIm) as a Function of Ligand Tilt and Bend^{*a*}

| ligand geometry | | shieldin | ig tensor e | isotropic | isotropic | |
|-----------------|---------------|------------------------------|--------------------------|--------------------------|----------------------------|------------------------|
| tilt (deg) | bend (deg) | <i>σ</i> ₁₁ (ppm) | σ ₂₂ (ppm) | σ ₃₃ (ppm) | shielding σ_i (ppm) | shift Δ_i (ppm) |
| 0 | 0 | -12266 | -11180 | -10961 | -11469 | 8547 |
| 0 | 20 | -12626 | -12032 | -11783 | -12147 | 9225 |
| 0 | 40 | -17295 | -16797 | -12126 | -15405 | 12483 |
| 20 | 0 | -12044 | -11271 | -10999 | -11438 | 8516 |
| 20 | 20 | -12330 | -11921 | -11542 | -11931 | 9009 |
| 20 | 40 | -14371 | -13772 | -12071 | -13404 | 10482 |
| 40 | 0 | -13900 | -12937 | -11236 | -12691 | 9769 |
| 40 | 20 | -14930 | -13947 | -11605 | -13494 | 10572 |
| 40 | 40 | -17521 | -16316 | -11982 | -15273 | 12351 |

^{*a*} Calculations were performed in Gaussian-94 using the B3LYP hybrid exchange correlation functional.

as described elsewhere.⁵⁰ The chromium carbonyl compounds were investigated with SOS-DFPT using the chromium DZVP (63321/5211/41+) basis set found in deMon,³⁹ IGLO–II basis sets on the remaining atoms, and the PW91 functional. The localized molecular orbital (LMO) contributions to the shielding in the Fe(C₂Cap)(CO)(NMeIm) model were calculated with SOS-DFPT using the iron DZVP (63321/5211/41+) basis set found in deMon,³⁹ IGLO–II basis sets on the other atoms, and the PW91 functional.

Small molecule calculations were carried out on International Business Machines (Austin, TX) RS/6000 computers (models 340, 350, 360, 365 and 3CT), while the larger systems were investigated using Silicon Graphics/Cray Research (Mountain View, CA) Origin 200, Origin-2000, and Power Challenge multiple processor machines. The geometry optimizations and ⁵⁷Fe shift and efg calculations were performed using the Silicon Graphics Power Challenge Array at the National Center for Supercomputing Applications, located in Urbana, IL, using up to 16 processors.

Results and Discussion

The rapid improvements in computer speed over the past few years, together with the increasingly widespread applications of density functional theory, strongly suggest that it should now be possible to compute a wide range of spectroscopic observables in metalloproteins and related model systems.⁵¹ The problem which exists, of course, is that the actual protein structures of interest are themselves the focus of debate. What is needed, therefore, are model compounds which have the same spectroscopic observables as do the proteins, but whose structures are more certain. Theoretical methods can then be used to predict the measured experimental parameters, validating the methods, after which aspects of protein structure can begin to be predicted using numerous observables measured on different proteins.

This is exactly the same approach which we have employed with amino acid residues in proteins in which quantum chemical methods were used to first reproduce chemical shifts (and shielding tensors) in amino acids⁵² and proteins;⁵³ the process was then "inverted" and structural information derived from the experimental results in both peptides²⁶ and proteins.²⁵ In work with peptides, the rms (root-mean-square) deviations between X-ray experiment and NMR prediction were ~11° for the

backbone torsion angles ϕ and ψ . In this work, we use up to seven different observables, as follows, which should give improved structural predictions:

1. $\delta_i^{13}C$ = the isotropic carbon-13 NMR chemical shift;

2. $\Delta \delta^{13}C$ = the ¹³C NMR chemical shift anisotropy, $|\delta_{33} - \delta_{11}|$, also known as the tensor breadth or span;

3. $\delta_i^{17}O$ = the isotropic oxygen-17 NMR chemical shift; 4. $e^2 q Q/h^{17}O$ = the oxygen-17 nuclear quadrupole coupling

constant; 5. δ_i^{57} Fe = the isotropic iron-57 NMR chemical shift;

- 6. $\Delta E_Q {}^{57}$ Fe = the iron-57 Mössbauer quadrupolar splitting;
- 7. ν_{CO} = the Fe-C-O infrared vibrational stretch frequency.

We consider first how the ¹³C, ¹⁷O, and ⁵⁷Fe NMR shift parameters vary with structure (tilt, τ , and bend, β), and we then investigate the accuracy of the experimental ¹³C tensor measurements, as well as how these tensors might be expected to vary as a function of axial base orientation and how individual localized molecular orbitals contribute to shielding. We then discuss experimental results on the Ao substate of MbCO, comparing them with experimental results obtained on a novel metalloporphyrin, Fe(5,10,15,20-tetraphenylporphyrin)(CO)(Nmethylimidazole), which has a linear and untilted Fe-C-O structure.²⁷ We then use a Bayesian probability or Z surface method^{25,26} to predict τ and β in the A_o substate of MbCO, followed by a related analysis of τ,β in the A₁ substate, where electrostatic field effects also influence v_{CO} and the ligand NMR parameters. Finally, we compare the results of calculations of the electrostatic field perturbations with experiment and conclude with a general model for the three conformational substates, A₀, A₁, and A₃, in terms of τ , β and electrostatics, which is consistent with all of the experimental results, an approach which should be applicable to other ligands as well.

Effects of Ligand Tilt and Bend on NMR Observables. We first consider the effects of ligand tilt and bend on the following spectroscopic observables: the ¹³C isotropic shift, the ¹³C shift anisotropy, the ¹⁷O isotropic shift, and the ⁵⁷Fe isotropic shift. Computed results for the model systems described above are given in Tables 1 and 2.

To begin with, we first compare these results with the experimental data published previously by ourselves and by others.^{14,21,54} In these previous studies, the ¹³C and ¹⁷O NMR observables for CO in picket fence porphyrin were reported^{14,21} in which CO is linear and untilted.⁵⁵ For ¹³C, at $\tau = \beta = 0^{\circ}$ the calculated values (converted from the absolute shieldings using a value of 186 ppm for the absolute shielding of tetramethylsilane, ref 56) are $\delta_{iso} = 215$ ppm, $|\delta_{22} - \delta_{11}| = 13$ ppm, and $|\delta_{33} - \delta_{11}| = 446$ ppm, to be compared with experimental values for the linear CO in picket fence porphyrin of $\delta_{iso} = 205$ ppm, $|\delta_{22} - \delta_{11}| = 8$ ppm, and $|\delta_{33} - \delta_{11}| = 457$ ppm. For ¹⁷O, the calculated values (converted from the absolute shieldings using a value of 306 ppm for the absolute shielding of liquid water, ref 57) are $\delta_{iso} = 392$ ppm, $|\delta_{22} - \delta_{11}| = 23$ ppm, and $|\delta_{33} - \delta_{11}| = 23$ δ_{11} = 757 ppm, to be compared with experimental values of $\delta_{\rm iso} = 372$ ppm, $|\delta_{22} - \delta_{11}| < 30$ ppm, and $|\delta_{33} - \delta_{11}| = 814$ ppm.¹⁴ The errors seen on the isotropic shift are those which are typically found when a range of organometallic compounds

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 Table 3.
 Computed ¹³C and ¹⁷O NMR Shielding Results for Chromium Carbonyls and Model Hemes

| system | σ_{11} (ppm) | σ_{22} (ppm) | σ_{33} (ppm) | $\sigma_{\rm i}$ (ppm) | $ \sigma_{11} - \sigma_{22} $ (ppm) |
|---|---------------------|---------------------|---------------------|------------------------|-------------------------------------|
| | | ¹³ C | | | |
| $Cr(CO)_5(pyr), 0^{\circ a}$ | -155.3 | -154.2 | 258.5 | -17.0 | 1.1 |
| Cr(CO) ₅ (pyr), 45° ^b | -155.4 | -154.4 | 258.2 | -17.2 | 1.0 |
| $Cr(CO)_5(NMeIm), 0^{\circ c}$ | -153.0 | -151.5 | 257.3 | -15.7 | 1.5 |
| $Cr(CO)_5(NMeIm), 45^{\circ d}$ | -153.4 | -152.1 | 257.6 | -15.9 | 1.3 |
| Fe(TPP)(CO)(pyr) ^e | -188.9 | -185.6 | 301.0 | -24.5 | 3.3 |
| Fe(TPP)(CO)(pyr) ^f | -188.6 | -186.1 | 298.8 | -25.3 | 2.5 |
| Fe(TPP)(CO)(NMeIm) ^g | -173.6 | -170.7 | 308.2 | -12.0 | 2.9 |
| Fe(TPP)(CO)(NMeIm) ^h | -199.2 | -196.5 | 308.2 | -29.2 | 2.7 |
| Fe(C ₂ Cap)(CO)(NMeIm) ⁱ | -196.6 | -194.1 | 312.9 | -25.9 | 2.5 |
| $Fe(C_2Cap)(CO)(NMeIm), 0^{\circ j}$ | -198.9 | -195.0 | 315.9 | -26.0 | 3.9 |
| Fe(C ₂ Cap)(CO)(NMeIm), 45° ^k | -198.3 | -195.8 | 314.6 | -26.5 | 2.5 |
| | | ¹⁷ O | | | |
| $Cr(CO)_5(pyr), 0^{\circ a}$ | -286.2 | -285.1 | 355.2 | -72.0 | 1.1 |
| Cr(CO) ₅ (pyr), 45° ^b | -285.9 | -283.2 | 355.5 | -71.2 | 2.7 |
| $Cr(CO)_5(NMeIm), 0^{\circ c}$ | -270.8 | -267.7 | 350.4 | -62.7 | 3.1 |
| Cr(CO) ₅ (NMeIm), 45° ^d | -272.4 | -269.0 | 369.6 | -63.0 | 3.4 |
| FeP(CO)(pyr) ^e | -284.5 | -281.8 | 421.1 | -48.4 | 2.7 |
| FeP(CO)(pyr) ^f | -287.0 | -283.5 | 419.1 | -50.4 | 3.5 |
| Fe(TPP)(CO)(NMeIm) ^g | -265.7 | -264.6 | 449.2 | -27.0 | 1.1 |
| Fe(TPP)(CO)(NMeIm) ^h | -333.1 | -331.6 | 446.5 | -72.7 | 1.5 |
| Fe(C ₂ Cap)(CO)(NMeIm) ⁱ | -317.6 | -316.2 | 447.5 | -62.1 | 1.4 |
| $Fe(C_2Cap)(CO)(NMeIm), 0^{\circ j}$ | -320.5 | -319.0 | 451.1 | -62.8 | 1.5 |
| $Fe(C_2Cap)(CO)(NMeIm), 45^{\circ k}$ | -320.3 | -318.4 | 449.0 | -63.2 | 1.9 |

^{*a*} Structure from ref 75, pyr plane along Cr $-C_{eq}$ axis, DZVP Cr/IGLO-II basis deMon calculation. ^{*b*} Structure from ref 75, pyr plane 45° to Cr $-C_{eq}$ axis, DZVP Cr/IGLO-II basis deMon calculation. ^{*c*} Structure from ref 75 with methylimidazole replacing pyridine, DZVP Cr/IGLO-II basis deMon calculation, NMeIm plane along Cr $-C_{eq}$ axis. ^{*d*} Structure from ref 75 with methylimidazole replacing pyridine, DZVP Cr/IGLO-II basis deMon calculation, NMeIm plane along Cr $-C_{eq}$ axis. ^{*d*} Structure from ref 75 with methylimidazole replacing pyridine, DZVP Cr/IGLO-II basis deMon calculation, NMeIm plane 45° to Cr $-C_{eq}$. ^{*e*} Structure from ref 28 (minus the C^{*β*}-substituents), Fe LANLD2DZ ECP/(42111/2111/311) basis set G94/DFT BPW91. See the text for details. ^{*f*} Structure from ref 28 (minus the C^{*β*}-substituents), Fe ECP/(42111/2111/311) basis set G94/DFT BPW91. ^{*s*} Structure from ref 27 (with the C_{meso} phenyl groups), riding model refinement, Wachters' Fe basis set, G94/DFT BPW91. ^{*h*} Structure from ref 60 (*minus* the ring substituents), Wachters' basis set, G94/DFT BPW91. ^{*i*} Structure from ref 60 (*minus* the ring substituents), Wachters' basis set, G94/DFT BPW91. ^{*i*} Structure from ref 60 (*minus* the ring substituents), Wachters' basis set, G94/DFT BPW91. ^{*i*} Structure from ref 60 (*minus* the ring substituents), Wachters' basis set, G94/DFT BPW91. ^{*i*} Structure from ref 60 (*minus* the ring substituents), Wachters' basis set, G94/DFT BPW91. ^{*i*} Structure from ref 60 (*minus* the ring substituents), Wachters' basis set, G94/DFT BPW91. ^{*i*} Structure from ref 60 (*minus* the ring substituents), Wachters' basis set, G94/DFT BPW91. ^{*i*} Structure from ref 60 (*minus* the ring substituents), Wachters' basis set, G94/DFT BPW91. ^{*i*} Structure from ref 60 (*minus* the ring substituents), Wachters' basis set, G94/DFT BPW91. ^{*i*} Structure from ref 60 (*minus* the ring substituents), Wachters' basis set, G94/DFT BPW91. ^{*i*} Structure from ref 60 (*minus* the ring subst

Table 4. Localized Molecular Orbital Contributions to CO Shielding in Fe(porphine)(CO)(N-methylimidazole)^{*a*}

| nucleus | LMO | σ_{11} | σ_{22} | σ_{33} | $\sigma_{\rm i}$ | $\Delta \sigma$ |
|-----------------|---------------------------|---------------|---------------|---------------|------------------|-----------------|
| ¹³ C | 1s(C) | 200.0 | 200.0 | 200.0 | 200.0 | 0 |
| | LP(O) | -53.4 | -53.3 | 3.3 | -34.5 | 56.7 |
| | $3 \times Bd(C \equiv O)$ | -88.6 | -88.5 | 39.9 | -45.7 | 128.5 |
| | $3 \times Bd(Fe-C)$ | -233.5 | -230.1 | 77.5 | -128.7 | 311.0 |
| | ΣAO(Fe) | 2.6 | 2.3 | -33.6 | -9.5 | -36.2 |
| | Σ^b | -172.9 | -169.6 | 287.1 | -18.4 | 460.0 |
| | total ^c | -168.9 | -166.1 | 308.4 | -8.9 | 477.3 |
| ¹⁷ O | 1s(O) | 270.1 | 270.1 | 270.1 | 270.1 | 0 |
| | LP(O) | -158.3 | -157.8 | 34.7 | -93.8 | 193.0 |
| | $3 \times Bd(C \equiv O)$ | -259.5 | -258.7 | 93.3 | -141.7 | 352.8 |
| | $3 \times Bd(Fe-C)$ | -157.5 | -154.7 | 30.3 | -93.9 | 187.8 |
| | ΣAO(Fe) | 0.4 | 0.3 | -7.0 | -2.1 | -7.4 |
| | Σ^b | -304.8 | -300.8 | 421.4 | -61.4 | 726.2 |
| | Total ^c | -299.0 | -295.7 | 425.4 | -56.4 | 724.4 |

^a Values given are in ppm and were determined with the deMon program. ^b Sum of 5 LMO contributions shown. ^c Total LMO contributions.

are investigated, since the absolute isotropic shieldings are typically in error by at least 10-20 ppm,^{58,59} and experimental errors on the individual tensor elements are also typically this large.⁶⁰ Thus, for these systems, there is generally good accord between theory and experiment. However, the known anticorrelation between ¹³C and ¹⁷O shifts seen in numerous proteins¹⁴ is not apparent in the calculated results. In addition, the large

(~80 ppm) anisotropies, $|\delta_{22} - \delta_{11}|$, seen in hemoglobin, myoglobin, and some model systems^{21,54,61} imply tilt angles between 30° and 40°. This translates to an 18 ppm difference in isotropic chemical shift, while the experimental difference between the protein and the picket fence porphyrin (linear) model is only 0.5 ppm. The results of Table 1 therefore indicate the following: (1) the calculations, structures, and/or theory have inadequacies, (2) some aspects of the shielding tensor measurements may be inaccurate, and/or (3) τ , β effects are unimportant in controlling the overall changes in ¹³C,¹⁷O shifts seen in different proteins.

The results obtained for the ⁵⁷Fe NMR chemical shifts are rather similar to those we found for the ¹³C,¹⁷O shift results given in Table 1 and are presented in Table 2. Experimentally, the isotropic chemical shift for ⁵⁷Fe in MbCO has been reported by us and by others to be at ~8227 ppm downfield from Fe-(CO)₅.^{32,62} The DFT shielding calculations indicate an ~8547 ppm deshielding for $\tau = \beta = 0^{\circ}$ (Table 2), but other τ , β values are also consistent with experiment. However, highly bent structures such as $\tau = 0$, $\beta = 40^{\circ}$ are some 4000 ppm too deshielded and are quite inconsistent with experiment. When taken together, the NMR results tend to support a linear geometry; therefore, we next investigate in more detail some of the NMR observations which tend to support nonlinearity.

The Question of $|\delta_{22} - \delta_{11}|$. One of the more puzzling results which emerges from the above calculations is that the large $|\delta_{22} - \delta_{11}|$ values, which have been seen experimentally

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Table 5. Experimental Determinations of Chemical Shift Tensor Elements in Mo(CO)₆ and Fe(TPP)(CO)(NMeIm)

| system | method | μ | ρ | δ_{11} (ppm) | δ_{22} (ppm) | δ_{33} (ppm) | $\delta_{ m i}$ (ppm) | $ \delta_{11} - \delta_{22} $ (ppm) |
|---------------------|----------------------------|-------|-------|---------------------|---------------------|---------------------|-----------------------|-------------------------------------|
| Mo(CO) ₆ | static | | | 338 | 338 | -72 | 201 | 0 |
| | least squares ^a | 11.71 | -0.91 | 346 | 328 | -71 | 201 | 18 |
| | Masfit ^b | 11.93 | -0.90 | 350 | 329 | -76 | 201 | 21 |
| | Z surface ^c | 11.4 | -1.0 | 336 | 336 | -70 | 201 | 0 |
| Fe(TPP)(CO)(NMeIm) | | | | | | | | |
| dry | Z surface ^c | | | 390 | 315 | -90 | 205 | 75 |
| solvated | Z surface ^c | | | 370 | 342 | -98 | 205 | 28 |

^{*a*} A least-squares fitting program kindly provided by R. E. Wasylishen. ^{*b*} A MAS NMR fitting program kindly provided by Alex Pines. ^{*c*} A Bayesian probability fitting program kindly provided by Dr. H. Le.

in several heme proteins and model compounds^{21,61} and have in proteins been attributed to geometric (τ,β) distortions,²¹ do not appear in the calculations. Or rather, when they do appear, they are accompanied by very large (\gtrsim 15 ppm) changes in isotropic shift from the linear, model compounds, effects which are not seen experimentally.

We therefore sought to see if such effects might be observable, computationally, in a series of model systems, by rotating the axial bases trans to CO, to see if, for example, metal $d\pi \rightarrow$ ligand π^* "back-bonding" effects might in some cases cause anisotropies in the ¹³C shielding tensor elements, a "proximal side" effect.³⁸ Results for Cr(CO)₅(pyridine) and Cr(CO)₅(*N*-methylimidazole) are presented in Table 3. Quite clearly, the anisotropies $|\sigma_{22} - \sigma_{11}|$ due to two different orientations (0°, 45°) of two ligands (pyridine, *N*-methylimidazole) cause at most a 1.5 ppm asymmetry of the shielding tensor of the *trans*-CO, although the effect is somewhat larger for the *cis*-COs (data not shown) and for the ¹⁷O shielding tensor elements as well, Table 3.

We next reasoned that the $Cr(CO)_5(B)$ model might simply be too crude a model to reproduce the effects seen in proteins, since it lacked the porphyrin macrocycle. We therefore investigated (a) a linear and untilted Fe-C-O system, FeP-(CO)(pyr), using two different Fe ECP/basis sets, resulting in a maximal $|\sigma_{22} - \sigma_{11}|$ of 3.3 ppm, and (b) two Fe(TPP)(CO)-(NMeIm) structures, one with an exact X-ray structure deduced using a riding model refinement⁶³ for the terminal CO, the second containing a DFT/G94 optimized Fe-C-O geometry, Table 3. The Fe P (pyr) structure contained a relatively planar porphyrin,⁶⁴ while that in the *N*-methylimidazole model is clearly saddled—but no effects on $|\sigma_{22} - \sigma_{11}|$ were seen. Finally, we investigated a structure based on $Fe(C_2Cap)(CO)$ -(NMeIm), an alternative close-to-planar porphyrin, using different axial base geometries, finding again only a 3.9 ppm maximal value for $|\sigma_{22} - \sigma_{11}|$, Table 3.

Interestingly, the anisotropies deduced using the Gaussian 94 program with the BPW91 functional tend to overestimate the $\Delta\sigma$ values seen experimentally, an effect which we have also noted in metal—olefin calculations.⁶⁵ We therefore investigated the ¹³C and ¹⁷O shieldings again, this time with a full planar porphyrin and a linear and untilted Fe–C–O fragment, using SOS-DFPT with the PW91 functional. Here, we again wished to see to what extent addition of a symmetry-breaking axial *N*-methylimidazole might be responsible for $\delta_{11} \neq \delta_{22}$. Results, together with the localized molecular orbital contributions to shielding, are given in Tables 3 and 4. For ¹³C, $|\sigma_{22} - \sigma_{11}| = 3.6$ ppm and, for ¹⁷O, $|\sigma_{22} - \sigma_{11}| = 3.3$ ppm, essentially the same results obtained with the Gaussian-94 calculations.

However, the $\Delta \sigma$ ¹³C result of 477.3 ppm is clearly closer to experiment, confirming previous observations on metal-olefin complexes which indicated somewhat more accurate ligand shieldings using the SOS-DFPT/IGLO approach.

The results of Table 4 are also of interest since they give a very simple breakdown of the localized molecular orbital (LMO) contributions to ¹³C,¹⁷O shielding. Apart from the 1s and lone pair contributions, both ¹³C and ¹⁷O shielding are dominated by C–O and Fe–C LMO contributions, with Fe–N_{im} and Fe–N_p contributions being quite minor. This, then, gives a logical explanation for the lack of major distal-base-orientation effects on the shieldings and emphasizes once again the unusual nature of observations of large $|\sigma_{22} - \sigma_{11}|$ values which have been reported in some systems. Such effects seem not to be possible on the basis of tilt–bend, since they would be accompanied by very large changes in isotropic shifts, and are also not due to proximal side effects.

We then began to investigate to what extent $|\sigma_{22} - \sigma_{11}|$ can actually be estimated using MAS NMR methods. As a first test, we reinvestigated the ¹³C shielding tensors in Mo(CO)₆. In previous work, we reported the spin-echo ¹³C NMR spectrum of a static sample of $Mo(^{13}CO)_6$, where it is quite clear that the shielding tensor is, as expected, axially symmetric with $\delta_{11} = \delta_{22} = 338$ ppm and $\delta_{33} = -72$ ppm, Table 4. However, two different MAS/SSB fitting programs indicated an appreciable asymmetry, $|\sigma_{22} - \sigma_{11}| = 18$ and 21 ppm, Table 5, using the MAS NMR sideband pattern reported previously.65 In contrast, a Bayesian probability based Z surface method gives $\delta_{11} = \delta_{22} = 336$ ppm and $\delta_{33} = -72$ ppm, Table 5, in good agreement with the static line shape simulation. The most probable reason for this observation is, we believe, that any errors in the fitting procedure, due for example to limited signalto-noise ratios, for an axially symmetric tensor will result in less than axial symmetry, in this case $|\sigma_{22} - \sigma_{11}| \approx 20$ ppm. Apparently, the Bayesian probability approach gives more accurate results in such situations, as demonstrated from the results presented in Table 5.

A second possible source of experimental error might originate from the sample itself. For example, in a dry sample there could be heterogeneity, due to crystallographic defects. We therefore investigated two samples of Fe(TPP)(CO)-(NMeIm), Figure 2. In Figure 2A, we show the ¹³C MAS NMR spectrum of a sample of Fe(TPP)(CO)(NMeIm) which had been dried in vacuo, while in Figure 2B we show a sample of crystals in excess mother liquor. The anisotropy seen in the dry sample is very large, $|\sigma_{22} - \sigma_{11}| = 75$ ppm, similar to that reported in some protein and metalloporphyrin samples,^{21,61} whereas in the solvated sample the anisotropy is considerably reduced to ~ 28 ppm, Figure 2, a value which is within a 10-15 ppm estimated uncertainty per tensor element of axially symmetric. Interestingly, there is essentially no change in the isotropic shift, which is at \sim 205 ppm in both cases, Table 4. The anisotropy of the two tensors, $|\sigma_{33}-\sigma_{11}|$, are very similar also, at 480 and 468 ppm.

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(65) Walter, T. H.; Thompson, A.; Keniry, M.; Shinoda, S.; Brown, T. L.; Gutowsky, H. S.; Oldfield, E. J. Am. Chem. Soc., 1988, 110, 1065-1068.



Figure 2. Experimental 90.5 MHz ¹³C CP-MAS NMR spectra of the A₀ heme model, Fe(TPP)(CO)(NMeIm). (A) Dry powder sample spectrum, 6 μ s 90° pulse widths, 5 ms mix time, ω_r = 3.462 kHz. (B) Solvated crystals, as in A but with ω_r = 3.1 kHz.

Therefore, it appears that while the isotropic shift and shift anisotropy can be quite reliably evaluated from MAS NMR spectra when using the Bayesian approach, $|\delta_{22} - \delta_{11}|$ values are clearly more difficult to estimate reliably and perhaps will be less useful in structural analysis for this reason, especially when used alone.

The A_o Substate. We next move on to consider just what information can be deduced about metal-ligand geometries in proteins by using NMR, Mössbauer, and IR spectroscopic results. We first consider the case of the A_o substate of myoglobin, or heme proteins in general. Here, it is important to make a connection between the results obtained with relatively well-characterized model compounds, and with data obtained on proteins.

Fortunately, the spectroscopic parameters for Fe(TPP)(CO)-(NMeIm) are very close to those found in the Ao substate of MbCO. The ^{13}C NMR spectrum of an Ao substate (tetrazole) MbCO sample is shown in Figure 3, from which we find that $\delta_i^{13}C = 205.8$ ppm and $|\sigma_{33}-\sigma_{11}| = 435$ ppm, values which are within experimental error the same as those found for Fe(TPP)-(CO)(NMeIm), $\delta_i = 205$ ppm and $|\delta_{33} - \delta_{11}| = 453$ ppm, Table 5. In addition, the ¹⁷O-isotropic shifts for A_0 proteins and the TPP model are very similar: $\delta_i^{17}O = 372$ ppm in the TPP model (exactly the same as found in solid $C^{\hat{1}\hat{7}}O$ picket fence porphyrin, ref 14) versus 372 \pm 1 ppm for a variety of A_o substate heme proteins.¹⁴ The ¹⁷O $e^2 qQ/h$ value in the TPP model from a nutation experiment, Figure 4, is 1.0 MHz, to be compared with 1.1 MHz on average for a range of Ao proteins from solution T_1 measurements,¹⁴ essentially the same as the 1.2 MHz we reported previously for C¹⁷O picket fence porphyrin from a line shape simulation.¹⁴ In addition, the ν_{CO} in the TPP model, 1969 cm^{-1} (data not shown) is also that found for A_o substate proteins.¹⁴ Finally, the ⁵⁷Fe Mössbauer quadrupole splitting of 0.35 mm \sec^{-1} in the TPP model⁶⁶ is close to that found in A_o substate mutant proteins (P. G. Debrunner, private communication). Taken together, these results tend to suggest that the linear Fe-C-O bonded Fe(TPP)(CO)(NMeIm) system



Figure 3. Proton-decoupled (90.46 MHz, 8.45 T) ¹³C MAS NMR spectrum of HisE7 tetrazoyl ¹³CO-myoglobin crystals obtained with ¹H cross polarization and nonquaternary suppression at a spinning speed of 3.4 kHz. Experimental conditions were -25 °C, 71 146 scans, 2 s recycle time, 3.9 μ s (90°) pulse width, 3 ms mix time, 60 μ s dephasing period (NQS), and 100 Hz line broadening due to exponential multiplication.



Figure 4. ¹⁷O NMR nutation plot for Fe(TPP)(CO)(NMeIm). The solution 90° pulse width (on H₂O) was 10.5 μ s. The nutation simulation yields $e^2 qQ/h = 1.0 \pm 0.2$ MHz, with an assumed asymmetry parameter $\eta = 0$.

and CO picket fence porphyrin, are good model systems for the A_o substates of heme proteins, since the ¹³C δ_i , ¹³C $|\sigma_{33}-\sigma_{11}|$, ¹⁷O δ_i , ¹⁷O e^2qQ/h , ν_{CO} , and ⁵⁷Fe ΔE_Q results are very similar. However, the possibility exists that there are other, alternative solutions for τ,β , which can also explain all of the spectroscopic observables, which we next investigate by using the Bayesian or Z surface approach.^{25,26}

The basic idea here is that if a parameter surface is computed as a function of tilt and bend, $P(\tau,\beta)$, then the likelihood that a given experimental value of a parameter, P^{expt} , is given by a particular set of τ,β values is given by^{25,26}

$${}^{1}Z = e^{-(P^{\text{expt}} - P^{\text{calcd}}_{\tau,\beta})^{2}/W}$$
(1)

where *W* is a search width parameter.^{25,26} If the computed value of the parameter, $P^{\text{calcd}}_{\tau,\beta}$ is identical to that found experimentally, $P^{\text{expt}} - P^{\text{calcd}}_{\tau,\beta} = 0$, then Z = 1, a high probability solution. On the other hand, if $P^{\text{expt}} - P^{\text{calcd}}_{\tau,\beta} \neq 0$, then $Z \to 0$, a low probability solution. The method can be readily extended from a one-parameter or ¹Z solution to multiple parameters, so long

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Figure 5. NMR parameter surfaces as a function of tilt and bend, computed using the deMon program with the Fe bis(amidinato)(CO)(*N*-methylimidazole) model system. (A) ¹³C-isotropic shielding surface, scaled to $\delta_i = 205$ ppm at $\tau = \beta = 0$, the experimental shift value for Fe-(TPP)(CO)(NMeIm) and picket fence porphyrin. (B) ¹⁷O-isotropic shielding surface, scaled to $\delta_i = 372$ ppm at $\tau = \beta = 0$. (C) ¹³C $\Delta\sigma$ ($|\sigma_{33} - \sigma_{11}|$) shielding anisotropy surface (ppm). (D) ¹⁷O NQCC surface (in MHz).

as the form of $P(\tau,\beta)$ is known. In this case, we investigate the use of four parameters: the ¹³C NMR isotropic chemical shift, the ¹³C NMR chemical shift anistropy, the ¹⁷O NMR isotropic chemical shift, and the ¹⁷O nuclear quadrupole coupling. The four Z surfaces are then combined as follows:

$${}^{4}Z(\tau,\beta) = {}^{1}Z({}^{13}C, \delta_{i}){}^{1}Z({}^{13}C, |\delta_{33} - \delta_{11}|){}^{1}Z({}^{17}O, \delta_{i}){}^{1}Z({}^{17}O, e^{2}qQ/h)$$
(2)

The actual computed parameter (P) surfaces are shown in Figure 5 and the individual ¹Z surfaces are shown in Figure 6. Here, it is important to note that the isotropic chemical shift surfaces have been converted from the chemical shifts computed theoretically using corrections of 10.3 ppm (¹³C) and 22.3 ppm (¹⁷O), such that the two known linear and untilted Fe(porphyrin)-(CO)(NMeIm) models have the experimental isotropic chemical shift. For the $|\delta_{33} - \delta_{11}|$ and ¹⁷O NQCC, this conversion was not necessary. In some Z surfaces, there are high probability solutions over wide regions of τ,β space, Figure 6. However, when all four parameters are simultaneously included, only the $\tau = \beta \leq 2^{\circ}$ region has a high probability, as shown in Figure 6. From this we conclude that the Ao substate of MbCO, and other heme proteins, has a linear Fe-C-O geometry. This is certainly not an unreasonable conclusion since all of the spectroscopic observables are virtually identical between A₀ MbCO and the new Fe(TPP)(CO)(NMeIm) model system. That is, a linear and untilted Fe-CO is one possible solution. However, the results of Figures 5 and 6, when considered together, are very important since they give no evidence for alternate τ,β conformational solutions which might also fit the experimental ¹³C and ¹⁷O NMR results.

The A_1 Substate. We next consider the A_1 substate of MbCO and other heme proteins, such as hemoglobin. Here, there are additional parameter surfaces to be considered. In

particular, there are several published results on the ⁵⁷Fe Mössbauer quadrupole splitting, ΔE_Q ,⁶⁷ as well as additional reports on the ⁵⁷Fe NMR isotropic chemical shift.^{32,62} We show in Figure 7 the ¹³C and ¹⁷O MAS NMR spectra of the A₁ substate of MbCO, from which we deduce δ_i , and for ¹³C, $|\delta_{33} - \delta_{11}|$ and these and other parameter results are collected in Table 6.

There are clearly isotropic chemical shift differences, in addition to ¹⁷O quadrupole coupling constant differences, between the A₀ and A₁ protein and model system results. These differences could, in principle, have two origins: either they are structural or they are electrostatic. In previous work, we and others have suggested an electrostatic origin for the observed frequency shifts and NQCC changes in the ligand atoms. The principal reason for this was that extremely good correlations are found between the various experimental parameters: δ_i ⁽¹⁷O), $\delta_i(^{13}\text{C})$, $e^2 q Q/h(^{17}\text{O})$, and ν_{CO} (14) (as shown for example in Figure 8). Here, we plot three correlations based on protein NMR/IR results, and in addition, we show the location of the new model compound, Fe(TPP)(CO)(NMeIm), Δ , as well as recent δ_1^{13} C/ ν_{CO} results for a C₂Cap porphyrin, which has highly perturbed frequency shifts.⁶⁸ Essentially all of the protein and model compound results lie on the same curves, implying a similar mechanism is responsible for these correlations. Indeed, with the inclusion of the C₂Cap results and results for the peroxidases, the correlation covers a range of almost 100 cm⁻¹ in $\nu_{\rm CO}$, Figure 8.

In earlier work, we reproduced to a modest extent the slopes of these correlations by using an electrostatic field to polarize a CO molecule: a model for MbCO. More recently, this model has been improved to include the electroneutral FeCO species

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Figure 6. Z surfaces as a function of tilt and bend for the A_0 substate of MbCO. (A) ¹³C-isotropic shift ¹Z surface. (B) ¹⁷O-isotropic shift ¹Z surface. (C) ¹³C CSA ¹Z surface. (D) ¹⁷O NQCC ¹Z surface. (E) ¹³C_{iso}, ¹³C_{CSA}, ¹⁷O_{iso}, ¹⁷O_{NQCC} ⁴Z surface. The values given are the likelihoods $\sqrt[n]{R_{CSA}}$.

shown in Figure 1A, and excellent accord was found for the ¹⁷O isotropic shift versus $\nu_{\rm CO}$ correlation and a more modest correlation for the ¹³C isotropic shift versus ν_{CO} correlation.^{14,36} We have now computed the ¹⁷O $e^2 q Q/h$ versus $v_{\rm CO}$ correlation, using both uniform field and point changes to perturb the FeCO fragment.⁶⁹ We find derivatives $\partial (e^2 q Q/h) / \partial (\nu_{CO})$ of 11 kHz/ cm⁻¹ for the uniform field model and 16 kHz/cm⁻¹ for the point charge model, to be compared with 11.28 kHz/cm⁻¹ determined experimentally.^{14,36,69} The averages of the uniform field and point charge IR/NMR correlation lines are shown in Figure 8 and strongly support the idea that E-fields determine the major changes seen between all the A_i substates, since the correlations between ${}^{13}C_i$, ${}^{17}O_i$, ${}^{17}O e^2 qQ/h$, and ν_{CO} are well reproduced by the calculations, although the absolute values of the properties are not exactly the same as the protein or porphyrin results because of the simplicity of the FeCO fragment.

Our results also suggest that *E*-field effects for the A_0 substate are close to zero, since there is no change in ν_{CO} in Fe(TPP)-(CO)(NMeIm) in solution and in the crystalline solid state and there is no distal fragment available to polarize the CO and generate an *E*-field effect.

If these ideas are correct, it should therefore be possible to extend the Bayesian probability approach to investigate the most likely conformation of the A₁ substate, simply by using the known $\nu_{\rm CO}$ to make a small correction to the observed ¹³C/¹⁷O shifts and the ¹⁷O e^2qQ/h values, using the theoretical correlation lines shown in Figure 8. In addition, for the A₁ substates of heme proteins, there is an extensive database of ⁵⁷Fe NMR chemical shifts and ⁵⁷Fe Mössbauer quadrupole splittings, ΔE_Q , which can also in principle be used to investigate τ , β effects.

We show therefore in Figure 9 computed ⁵⁷Fe NMR isotropic chemical shift and ⁵⁷Fe Mössbauer quadrupole splitting surfaces as a function of τ , β for a model Fe(P)(CO)(NMeIm) metallo-

(69) deDios, A. C.; Earle, E. Unpublished results.

cycle. The ⁵⁷Fe NMR chemical shieldings, Figure 9A, computed using the G94/DFT GIAO method described above are given in Table 3 and have been converted into ⁵⁷Fe NMR chemical shifts, δ_i , in ppm from Fe(CO)₅ using the following equation

⁵⁷Fe
$$\delta$$
(shift, ppm from Fe(CO)₅) = -2922 - σ (calcd, ppm)
(3)

where σ (calcd, ppm) is the isotropic shielding given in Table 2. The value of -2922 ppm has been established by using the databases of Bühl (50) augmented with three model calculations on metallocycles Fe(TPP) (Me₂S)(NMeIm), Fe(TPP)(ⁱPrNC)-(NMeIm) and Fe(TPP)(CO)(NMeIm), using the experimental shifts of cytochrome c,⁷⁰ alkyl isocyanide myoglobins and carbonmonoxymyoglobin, as will be described in detail elsewhere.⁷¹

The Mössbauer quadrupole splittings are derived from the electric-field gradient tensor, computed in Gaussian-94 using the B3LYP hybrid exchange correlation functional. In Mössbauer spectroscopy, the observed spectra of low spin d⁶ iron complexes generally consist of a quadrupole split doublet having a peak separation, ΔE_Q , which is related to the elements of the electric field gradient tensor at the nucleus by

$$\Delta E_{\rm Q} = \frac{1}{2} e Q V_{zz} \left(1 + \frac{\eta^2}{3} \right)^{1/2} \tag{4}$$

where *e* is the electron charge, *Q* the quadrupole moment of the $I^* = {}^{3}/_{2}$, 14.4 keV excited state, V_{zz} is the largest component of the efg tensor, and by convention

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Table 6. Experimental Parameters for Fe(TPP)(CO)(NMeIm), A₀ and A₁ Myoglobins

| system | ¹³ C _i (ppm) | ¹³ C _{CSA} (ppm) | ¹⁷ O _i (ppm) | ¹⁷ O _{NQCC} (MHz) | ⁵⁷ Fe _i (ppm) | $\Delta E_{\rm Q} ({\rm mm/s})$ | IR (cm ⁻¹) |
|--|---|--------------------------------------|-------------------------------------|---------------------------------------|-------------------------------------|----------------------------------|--|
| Fe(TPP)(CO)(NMeIm) A ₀ myoglobin A ₁ myoglobin | 205.0^{a} 205.5^{d} 207.2^{d} | 453^{a} 435^{a} 447^{a} | 372^{a} 372^{d} 366^{a} | ${1.0^a} \ {1.1^d} \ {0.8^d}$ | 8227 ^e | 0.35^{b} 0.37^{f} | 1969 ^c 1969 ^d 1944 |

^a Determined in this work. ^b Reference 66. ^c Determined in Nujol. ^d Reference 14. ^e Reference 32. ^f Reference 22.

$$\eta = \frac{V_{xx} - V_{yy}}{V_{zz}} \tag{5}$$

$$|V_{zz}| > |V_{yy}| > |V_{xx}| \tag{6}$$

In the presence of an applied field, each molecule has its efg oriented differently in the field, and a powder spectrum is observed. However, methods are available to evaluate such powder averages as a function of V_{ii} , from which ΔE_Q and the sign of ΔE_Q can be deduced.^{72,73} Unfortunately, there has been some debate as to the value of Q, the quadrupole moment of the excited iron nucleus. Here, we use a recent and reportedly very precise value, $Q = 0.16 \times 10^{-28}$ cm², to convert the computed V_{ii} values (in atomic units) to the Mössbauer quadrupole splittings, ΔE_Q (mm/s) using eq 4.

Elsewhere, we have investigated the ⁵⁷Fe Mössbauer quadrupole splittings in 14 organometallic model systems⁶⁶ and find a <0.2 mm/s rms error between theory and experiment, which gives an idea as to the accuracy with which ΔE_0 can be determined. Figure 9B shows the Mössbauer $\Delta E_0(\tau,\beta)$ surface computed for our model metalloporphyrin. In separate work, we have found experimentally⁶⁶ that the quadrupole splitting of the model system Fe(5,10,15,20-tetraphenylporphyrin)(CO)-(N-methylimidazole) is 0.35 mm/s, essentially the same as that seen in MbCO, where values of 0.363-0.373 have been reported.^{23,67} Large basis set efg calculations on the complete TPP system yield a ΔE_0 of 0.44 mm/s, to be compared with our smaller model, having $\Delta E_Q = 0.52 \text{ mm/s}.^{66}$ Since we know that the linear Fe–C–O TPP model has a 0.35 mm/s ΔE_Q , we have used a -0.17 mm/s correction to the τ , $\beta \Delta E_Q$ surface. This is necessary, since otherwise we would conclude the TPP model is slightly bent, which it is not-although we should note that even an unscaled (0.52 mm/s $\tau = \beta = 0^{\circ}$) surface only changes the final τ,β predictions by about 1°.

For the iron-57 NMR chemical shift, the ¹Z surface, Figure 9C, shows a most likely solution close to $\tau = \beta = 0^{\circ}$, although given the 800 ppm rms error seen for three metalloprotein models⁷¹ (as reflected in our 787 ppm value for *W*), clearly considerable distortions are allowed, based solely on the ⁵⁷Fe NMR chemical shift. The same can be said for the iron-57 Mössbauer ΔE_Q ¹Z surface, Figure 9D. For example a $\tau = \beta = 20^{\circ}$ solution is spectroscopically permissible, albeit not so energetically. These results simply reinforce the idea that multiple *Z* surfaces need to be combined in order to obtain a τ , β solution which is consistent with *all* of the observables. We therefore show in Figure 10 the ⁶Z surface obtained by considering all of the NMR and Mössbauer data:

$${}^{6}Z(\tau,\beta) = {}^{1}Z({}^{13}C, \delta_{i}){}^{1}Z({}^{13}C, CSA){}^{1}Z({}^{17}O, \delta_{i}) \times {}^{1}Z({}^{17}O, e^{2}qQ/h){}^{1}Z({}^{57}Fe, \delta_{i}){}^{1}Z({}^{57}Fe, \Delta E_{O})$$
(7)

The most likely solution occurs for $\tau = 4^{\circ}$, $\beta = 7^{\circ}$, essentially a linear and untilted Fe–C–O fragment. This result gives good predictions for the isotropic ¹³C NMR chemical shift, the ¹³C



Figure 7. Experimental ¹³C and ¹⁷O solid-state MAS NMR spectra of A₁ CO horse myoglobin crystals at pH 7. (A) ¹³C CP-NQS NMR spectrum at 90.5 MHz, -25 °C, 7 μ s 90° pulse widths, 60 μ s dephasing, a 3 ms mix time, $\omega_r = 3.7$ kHz, recycle = 2 s, 88 944 scans, convolution difference processing. (B) 67.8 MHz (11.7 T) ¹⁷O NMR spectrum of C¹⁷O-myoglobin crystals. Experimental conditions were -24 °C, 1 048 000 scans, 50 ms recycle time, a 5.0 μ s (solid 90°) pulse width, and 25 Hz line broadening due to exponential multiplication. The spinning sidebands are numbered.

NMR chemical shift anisotropy, the isotropic ¹⁷O NMR chemical shift, the ¹⁷O nuclear quadrupole coupling constant, the ⁵⁷Fe NMR chemical shift, and the 57Fe Mössbauer quadrupole splitting, as summarized in Table 7. Moreover, the result shown in Figure 10 is not dominated by a single, narrow solution for a particular spectroscopic parameter. For situations in which there are extensive amounts of data, for example ¹³C NMR shifts of amino acid residues in proteins, the W value chosen in eq 1 can be related to the rms or standard deviation of the data set.^{25,26} However, when only single-point experiments are available, W values have to be deduced by estimating errors on a calculation (and experiment) in the absence of a large body of data. In such situations, a single badly chosen W value may dominate the final Z surface. We have tested for this possibility by selectively removing individual Z surfaces from the result shown in Figure 10, to generate the six individual ⁵Z surfaces shown in Figure 11. In all cases, the ${}^{5}Z$ results are very similar to the ⁶Z results, with τ,β values very similar to the ⁴Z result obtained with the A_0 substate, Figure 6. That is, in no case does a single Z surface dominate the final result. The actual W-values used, together with a theoretical-versus-experimental comparison of

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Figure 8. Experimental (solid circles, from ref 14) and theoretical (solid lines, from refs 36 and 69) NMR/IR correlation plots for heme proteins and model compounds. (A) ¹³C-isotropic shift versus ν (C–O). (B) ¹⁷O-isotropic shift versus ν (C–O). (C) ¹⁷O NQCC versus ν (C–O). The solid circles represent results obtained on proteins. The open triangles are the results obtained on the TPP model described in the text, and the open square is C_2 -cap. The solid lines are the theoretical correlation lines, based on Fe–C–O model systems^{36,69} offset along the ordinate to intersect the data at $\nu_{CO} = 1969 \text{ cm}^{-1}$, to facilitate comparison.



Figure 9. ⁵⁷Fe NMR isotropic chemical shift and Mössbauer quadrupole splitting tilt-bend surfaces and associated *Z* surfaces for the A₁ substate. (A) ⁵⁷Fe-isotropic shift parameter surface. (B) ⁵⁷Fe quadrupole splitting parameter surface, offset by -0.17 mm/s to reproduce the Fe(TPP)(CO)-(NMeIm) model system. (C) ⁵⁷Fe-isotropic shift ¹Z surface. (D) ⁵⁷Fe quadrupole splitting ¹Z surface. The values shown in A are the ⁵⁷Fe shifts, in 10³ ppm, and in B are the ΔE_Q in mm/s. The values in C and D are the ¹Z likelihoods.

all of the results obtained, are given in Table 7. Note that both τ,β and E-field contributions are included. On average, the mean ${}^{13}C, {}^{17}O =$ isotropic shift error is 0.4 ppm, the ${}^{13}C$ CSA error is 7 ppm, the efg error is 0.13 MHz, the ⁵⁷Fe ΔE_0 error is 0.05 mm/s, and the ⁵⁷Fe-isotropic shift error is 179 ppm. For the ¹³C and ¹⁷O shifts, as noted previously, the isotropic shifts were scaled to fit the linear TPP and picket fence models, as was the ⁵⁷Fe Mössbauer surface. This is necessary in part to account for basis and functional deficiencies and is similar to the scaling we have used previously with amino acid shielding in peptides²⁶ and proteins.²⁵ For the ¹³C CSA, the ¹⁷O NQCC, and the ⁵⁷Fe shifts, no scaling was used since the CSAs and efgs were in good accord with the model compound experiments, and for ⁵⁷Fe, the solid-state ⁵⁷Fe shift is unknown. Indeed, the use of solely unscaled and uncorrected parameter surfaces yields $\tau = \beta = 6^\circ$, in good agreement with the more rigorous computations described above.



Figure 10. ⁶Z surface for A₁ protein conformational substate using ¹³C δ_i , ¹⁷O δ_i , ⁵⁷Fe δ_i , ¹³C $\Delta\delta$, ¹⁷O NQCC, and ⁵⁷Fe ΔE_Q surfaces. The maximum is at $\tau = 4^\circ$, $\beta = 7^\circ$. The maximum Z value is ${}^6\sqrt{{}^6Z} = 0.92$.



Figure 11. Six ⁵Z surfaces of A₁ myoglobin illustrating the effect of removing each Z surface. **A**, ¹³C isotropic shift removed. **B**, ¹⁷O isotropic shift removed. **C**, ⁵⁷Fe isotropic shift removed. **D**, ¹³C CSA removed. **E**, ¹⁷O NQCC removed. **F**, ⁵⁷Fe quadrupolar splitting removed. The countours represent $\sqrt[5]{5Z}$ and decrease in 0.1 intervals.

Table 7. Calculated and Experimental Spectroscopic Parameters for Typical A_0 and A_1 CO–Heme Protein Substates

| | | A_0 | | A ₁ | | | |
|---|------------|--------------|-----|----------------|--------------------|------------|--|
| parameter | calcd | exptl | W | calcd | exptl ^a | W | |
| $^{13}C_{iso} (ppm)$ | 205 446 | 205.3 435 | 3.2 | 206.8 445 | 207.2 | 3.2 | |
| ¹⁷ O _{iso} (ppm) | 372 | 372.4 | 4.5 | 366.7 | 366 | 4.5 | |
| $^{17}O_{NQCC}$ (MHz) $^{57}Fe_{\Lambda E_{O}}$ (mm/s) | 0.9 | 1.1 | 0.6 | 0.64 0.30 | 0.8 0.37 | 0.6 0.4 | |
| ⁵⁷ Fe _{iso} (ppm) | | | | 8406 | 8227 | 787 | |

^{*a*} The electrical contributions to ¹³C δ_i , ¹⁷O δ_i and the ¹⁷O NQCC were obtained from the theoretical correlation lines shown in Figure 8.

In summary then, the use of density functional theory now permits the relatively accurate prediction of ¹³C NMR chemical shifts and shift tensor elements, ¹⁷O NMR shifts, ¹⁷O nuclear quadrupole coupling constants, 57Fe NMR chemical shifts and ⁵⁷Fe Mössbauer quadrupole splittings in metalloporphyrin model systems and in metalloproteins themselves. Experimental results on linear and untilted Fe-C-O metalloporphyrins are essentially the same as those found in the A₀ substate of heme proteins. This implies that the proteins could also contain linear and untilted Fe-C-O units, and the results of additional DFT calculations rule out alternative, distorted conformations for the A_0 substate. With the A_1 substates of heme proteins, there are small changes in the ligand NMR and electric field gradient parameters, but these can now be rather well described, especially for the δ_i ¹⁷O and ¹⁷O NQCC/ ν_{CO} correlations, in terms of purely electrostatic field effects, calculable via quantum chemistry. For the A₁ substate, we also have available the ⁵⁷Fe NMR isotropic shifts and the 57Fe Mössbauer quadrupole splittings, ΔE_0 . These are not expected to change appreciably with E-field effects, since these in general come from the distal histidine and as such are expected to affect primarily the ¹⁷O shift and ¹⁷O NQCC. The ⁵⁷Fe shift and ⁵⁷Fe efg can therefore be used as additional parameters with which to test ideas about metal-ligand geometry. Using the simple porphyrin model, we find errors of about 200 ppm for the 57Fe shift (8227 ppm expt, 8406 ppm calcd), a small number when compared with the $\sim 1000-3000$ ppm errors found for 20°, 40° bent geometries. The same can be said for the 57Fe Mössbauer results, wherehighly bent geometries result in very large errors in computed ⁵⁷Fe efgs, while linear and untilted geometries give computed Mössbauer quadrupole splittings, ΔE_0 , which are very close to those found experimentally.

We believe these results therefore indicate that the A₀ and A₁ substates of MbCO and, by inference other heme proteins, contain linear Fe-C-O geometries, since all six spectroscopic observables: the carbon-13, oxygen-17, and iron-57 NMR isotropic chemical shifts, the ¹³C shift anisotropy, the ¹⁷O quadrupole coupling constant, and the ⁵⁷Fe Mössbauer quadrupole splitting, are all close to those found via DFT. This improves upon the more limited results using just DFT energies alone or solely IR data, which appear to leave some uncertainties as to the actual τ,β values present in proteins, with in some cases large distortions reported as possible (see, e.g., ref 74). The changes in the ligand NMR/IR shifts from system to system seen previously can be readily accounted for in terms of E-field effects, again using DFT methods. These results also suggest that the A₃ substate is very close to linear and untilted, as are the unusually shifted peroxidase "post-A3" substates, since (i) all points fall on the universal $\delta_i^{17}O/\delta_i^{13}C/^{17}O$ NQCC/ ν_{CO} correlations, (ii) the slopes of these correlations can now be computed via use of DFT methods, and (iii) these correlations are not due to τ,β .

While an argument might be made that the highly distorted Fe-C-O structures are only found in $P2_1$ sperm whale MbCO, the Mössbauer surface results give no support to this idea, and indeed DFT calculations at the X-ray geometries overestimate ΔE_Q by 500%,⁶⁶ while assumption of a linear geometry gives results within the 0.1-0.2 mm/s rms error expected. Indeed, the fact that both solution and solid-state data can all be combined together using the Bayesian probability approach to give unique solutions, which permit an explanation of seven different observables from three different spectroscopies, NMR, IR, and Mössbauer, which also cover a dozen or more proteins and model systems (C₂Cap, A₀, A₁, A₃, peroxidases), gives some confidence in the use of such methods for investigating related structural questions in other systems as well.

Conclusions

The results we have shown above are of interest for three reasons. First, they represent the first comprehensive investigation of ¹³C NMR chemical shifts, ¹³C NMR chemical shift

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anisotropies, ¹⁷O NMR chemical shifts, ¹⁷O nuclear quadrupole couplings, ⁵⁷Fe NMR chemical shifts, and ⁵⁷Fe Mössbauer quadrupole splittings in metalloproteins and model systems using modern density functional methods and experiment. Second, our results indicate that all of the spectroscopic observables can be well accounted for in terms of linear, untilted Fe-C-O bonding, with weak electrostatic fields controlling the differences seen between A₀ and A₁ substates. Third, we have extended the use of the Z surface method, based on Bayesian probability, to explore the topic of ligand tilt and bend: the results give no support for distorted geometries, either in solution or in the solid-state. Combining the results of NMR, IR, and Mössbauer spectroscopic measurements in this way should be a general approach for predicting metal-ligand geometries in other systems as well, for example with O₂ and RNC metalligand bonding in heme proteins, where the more conventional IR/Raman-based methods alone are less sensitive.

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